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# Origin of Dark Energy in the Universe: Can D-instanton Source a Quintessence?

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**ABSTRACT:** Can a *D*-instanton provide a clue to the origin of dark energy in universe? In the context we briefly review our construction for a string-brane model which underlies a vacuum created gravitational pair of  $(3\overline{3})$ -brane by a Kalb-Ramond (KR) field on a  $D_4$ -brane. Obtained results reveal that a dynamical *D*-instanton could be quintessential to incorporate a non-perturbative quantum correction to (3+1)-dimensional brane universe. It provokes thought to believe that an extra fifth spatial dimension to the brane universe can be sourced by a *D*-instanton which could be a potential candidate to source the enormous dark energy.

KEYWORDS: Cosmological Pair Production, Kalb-Ramond Field, Quantum Gravity, String Theory, D-instanton

# I. INTRODUCTION: STRINGY APPROACHES TO QUANTUM GRAVITY

Black holes are described in Einstein gravity which underlies an intrinsic metric dynamics on a Riemannian manifold. Interestingly the stringy versions of these macroscopic black holes have been obtained in a low energy limit of a string effective action in the past [1, 2, 3, 4, 5]. In fact, a nontrivial background metric on a string world-sheet is known to incorporate vertex operators in a path integral and hence naturally introduces a string coupling at each interaction vertex. A weak coupling consistently incorporates perturbative geometric (higher genus) corrections to the string world-sheet at tree level and leads to a theory of quantum gravity.

On the other hand the quantum effects to Einstein gravity can also be explored addressed non- perturbatively using the strong-weak coupling duality in ten dimensional superstring theories [6]. A non-perturbative quantum effect is believed to be sourced by compactified extra space dimension(s) to various stringy vacua. In particular, the type IIA superstring theory in a strong coupling limit is known to incorporate an extra spatial dimension on  $S^1$  and has been identified with the non-perturbative *M*-theory in eleven dimensions. Generically *M*-theory has been shown to be identified with the stringy vacua in various dimensions [7]. In a low energy limit M-theory is known to describe an eleven dimensional supergravity. However a complete non-perturbative formulation of *M*-theory is not known.

# II. PAIR CREATION OF $(3\overline{3})$ -BRANE UNIVERSE AT BIG BANG

**PERSPECTIVES:** We begin by briefly revisiting the Schwinger pair production mechanism [8] established in quantum field theory (QFT). The novel idea elegantly describes a positron and electron pair production at a QFT vacuum by electromagnetic quanta, i.e. photon. The pair production mechanism is an emergent non-perturbative phenomenon. It is believed to be instrumental to describe diverse quantum phenomenon in gravitation and cosmology. In fact the tool was explored to explain the Hawking radiation phenomenon [9], where an incident photon generates a pair of charged particle/anti-particle at the event horizon of a black hole. Furthermore the idea was applied to the open strings pair production by Bachas and Poratti [10]. Majumdar and Davis have exploited the underlying mechanism to investigate the production of a higher dimensional pair of  $(D\overline{D})_9$  at the cosmological horizon [11].

An extra spatial dimension compactified on  $S^{l}$  has been argued to unfold in the ten dimensional type IIA superstring theory when the string coupling becomes large. As a result the strong coupling string theory has been conjectured to describe an eleven dimensional non-perturbative *M*-theory. Interestingly the emergent curvature on a pair of brane/anti-



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brane was shown to be described by a geometric torsion in a string-brane model [12, 13, 14]. The model may be viewed as an attempt to explore the non-perturbative domain in quantum gravity underlying a string theoretic setup. Importantly the torsion geometry underlying a (4+1)-dimensional world-volume gauge theory was generalized to (5+1)-dimensional CFT to describe a gravitational pair of de Sitter (4 $\overline{4}$ )-brane universe [15, 16]. In principle the mechanism may be explored on a pair of  $(D\overline{D})_9$ -brane at a strong coupling to gain insight into the conjectured *M*theory. A preliminary investigation, using the brane/anti-brane production tool by a higher form, in an appropriate pbrane world-volume theory has been performed [17] to enhance our knowledge on the M-theory.

STRING-BRANE MODEL: DYNAMICAL NS FIELD: In the recent past the string-brane model underlying a geometric torsion was constructed to address a non-perturbative [18] quantum correction to the low energy string vacuum [12, 13, 14]. It was shown that non-BPS brane may well be described by a non-perturbative phenomenon leading to a vacuum created gravitational pair of  $(D\overline{D})_3$ -brane by the KR quanta on a  $D_4$ -brane at the cosmological horizon of a background de Sitter brane geometry. The absorption of the KR field in the five dimensional U(1) gauge theory was shown to modify the covariant derivative, which in turn describes an emergent torsion curvature on a pair. Alternately, KR field local degrees have been transformed to project a dynamical NS field on a vacuum created non-BPS pair of  $(D\overline{D})_3$ -brane which presumably defines our early universe. The momentum conservation ensures that the vacuum created gravitational 3-brane and  $\overline{3}$ -brane cannot annihilate each other and defines a stable pair of (3+1)dimensional brane/anti-brane universe. In fact, the cosmological creation of a pair of non-BPS  $(D\overline{D})_{9}$ -brane in a different context was discussed by Majumdar and Davis [11]. Their work was primarily motivated to address the strong coupling regime in type IIA superstring leading to the *M*-theory. A brief outline to exploit the strength of a string-brane model for an enhanced understanding of the *M*-theory has been discussed in ref. [17]. It is worth mentioning that a pair of brane and anti-brane is known to break the supersymmetry and hence is described by a non-BPS brane. Past analysis has revealed that some of the non-BPS states are stable in superstring theories [19]. It was shown that the (open string) tachyon condenses on a non-BPS brane to describe a stable pair of  $(D\overline{D})$ -brane [20].



In the context the vacuum refers to an open string background black hole on a  $D_4$ -brane which is known to be sourced by a constant NS field [21] in the string bulk. The KR field quanta is believed to vacuum create a pair of  $(1\overline{1})$ -brane instead of a charged pair of particle and anti-particle. Their stability favours an increase in the number of their spatial dimensions. Finally, they describe a space filling gravitational pair of  $(3\overline{3})$ -brane underlying the (4+1)-dimensional world-volume gauge theory. The KR field dynamics is given by

$$S = -\frac{1}{12C_2^2} \int d^5 x \sqrt{-G^{(NS)}} H_{\mu\nu\lambda} H^{\mu\nu\lambda}, \quad \text{where } C_2^2 = \left(8\pi^3 g_s\right) \alpha'^{3/2} \quad . \tag{1}$$

The significance of the constant NS field in addition to the local KR field has been addressed in an effective curvature formalism on a  $D_4$ -brane [22, 23, 24, 12, 13, 14]. Importantly  $H_3$  has been identified with a connection which in turn



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modifies the covariant derivative to  $\mathcal{D}_{u}$  on a D<sub>4</sub>-brane. The mathematical construction implies an absorption of KR field quanta and hence the  $\mathcal{D}_{\mu}$  describes a "fat" brane or a string-brane model. In other words the model evolves with a dynamical NS field at the expense of the KR field on a  $D_4$ -brane. As a result the emergent pair of brane-universe is governed by a geometrical torsion:

$$H_{\mu\nu\lambda} = \mathfrak{D}_{\mu}B_{\nu\lambda}^{NS} + \text{cyclic} = (H_{\mu\nu\alpha}B_{\lambda}^{(NS)\alpha} + \text{cyclic}) + H_{\mu\nu\beta}B_{\alpha}^{(NS)\beta}B_{\lambda}^{(NS)\alpha}$$
  
Where 
$$\mathfrak{D}_{\lambda}B_{\mu\nu}^{NS} = \frac{1}{2}H_{\lambda\mu}^{\rho}B_{\rho\nu}^{NS} - \frac{1}{2}H_{\lambda\nu}^{\rho}B_{\rho\mu}^{NS}, \nabla_{\lambda}B_{\rho\nu}^{NS} = 0.$$
 (2)

It shows that the geometric torsion underlies a fat brane which breaks the supersymmetry. Thus it describes a non-BPS pair of emergent gravitational (33)-brane. The presence of string bulk due to the dynamical NS field ensures the closed string modes coupling to the otherwise BPS brane. Importantly, the geometric torsion in the string-brane model is exact and hence is non-perturbative. In addition, the U(1) gauge invariance of a geometric torsion under a two form transformation has been realized in an effective space-time curvature formalism. A dynamical space-time without a torsion in 4-Dimensions has been argued to begin at a Big Bang singularity defined at a cosmological horizon. It is noteworthy to remark that the space-time curvature sourced by a geometric torsion in 5D naturally incorporates an intrinsic angular momentum on a vacuum created pair of  $(D\overline{D})_3$ -brane. The world-volumes of a brane and an anti-brane are separated by an extra fifth dimension transverse to each other. It may imply that an observer in a  $D_3$ -brane universe is inaccessible to an anti  $D_3$ -brane universe or vice-versa. Nevertheless, the hidden effect of an anti  $D_3$ -brane space-time via an extra dimension is indeed compelling on a 3-brane universe. Analysis may reveal that a brane universe geometry appears to be influenced by an axion which is a potential candidate to source the dark energy.

## **NON-PERTURBATIVE QUANTUM GRAVITY: EMERGENT METRIC**

The commutator  $[\mathcal{D}_{\omega} \ \mathcal{D}_{\nu}]$  is worked out to yield a fourth order reducible torsion curvature tensor in a second order formalism [12] underlying a vacuum created gravitational pair of  $(3\overline{3})$ -brane [13]. With an appropriate rescaling of  $\frac{1}{2}\mathcal{H} \to \mathcal{H}$ , the emergent torsion curvature tensor takes a form:

$$\widetilde{K}^{\rho}_{\mu\nu\lambda} = \partial_{\mu}\mathcal{H}^{\rho}_{\nu\lambda} - \partial_{\nu}\mathcal{H}^{\rho}_{\mu\lambda} + \mathcal{H}^{\sigma}_{\mu\lambda}\mathcal{H}^{\rho}_{\nu\sigma} - \mathcal{H}^{\sigma}_{\nu\lambda}\mathcal{H}^{\rho}_{\mu\sigma}(3)$$

The fourth order tensor is antisymmetric under an exchange of indices within a pair and is not symmetric under an exchange of its first pair of indices with the second. It differs from the Riemannian tensor  $R_{\mu\nu\lambda\rho}$ . However for a nonpropagating torsion  $\tilde{K}_{\mu\nu\lambda\rho} \rightarrow R_{\mu\nu\lambda\rho}$ . The irreducible torsion curvature scalar  $\tilde{K}$  is worked out on  $S^{I}$  to describe a vacuum created gravitational pair of (33)-brane. Then, the local dynamics is approximated by two independent 4-Dim curvatures and is given by

$$S_{(3-\bar{3})} = \frac{1}{12\mathcal{K}^2} \int d^4x \sqrt{-g} K - 3 \bar{\mathcal{F}}_{\mu\nu} \mathcal{F}^{\mu\nu}$$
(4)

where  $\mathcal{F}_{\mu\nu} = (\mathcal{D}_{\mu}A_{\nu} - \mathcal{D}_{\nu}A_{\mu}) = F_{\mu\nu} + \mathcal{H}^{\alpha}_{\mu\nu}A_{\alpha}$ . The U(1) gauge invariance of the Lorentz scalar  $\mathcal{H}^2$  has been shown to incorporate a metric fluctuation  $f^{q}_{\mu\nu} = C(2\pi\alpha') H^{\mu}_{\ \alpha\beta}\mathcal{H}^{\alpha\beta}_{\nu}$  to the background open string metric. It takes a form:  $G_{\mu\nu} = (G^{(NS)}_{\mu\nu} + C \overline{\mathcal{H}}_{\mu\lambda\rho}\mathcal{H}^{\lambda\rho}_{\nu})(5)$ where  $B_{\mu\nu}$  signifies a constant NS field and appropriately couples to an electromagnetic field  $F^{linear}_{\ \mu\nu}$  to retain the U(1)gauge invariance. Thus  $f^{q}_{\ \mu\nu}$  incorporates a non-perturbative correction to the open string metric established on a Dbrane [21]. Interestingly a low energy limit in the string- brane model corresponds to a non-propagating geometric torsion and hence the emergent scenario on a pair of (33)-brane is described with a large extra dimension. Then a Dbrane or an anti D-brane correction, sourced by a geometric torsion, may be ignored to describe Einstein vacuum in the string-brane model. A fact that a torsion is dual to an axion on a gravitational 3-brane ensures one degree of freedom. In addition  $\mathcal{F}_{\mu\nu}$  describes a geometric one form field with two local degrees on a gravitational 3-brane. A precise match among the (three) local degrees of torsion in  $\tilde{K}$  on  $S^{l}$  with that in K and  $\mathcal{F}_{\mu\nu}$  reassure the absence of a dynamical dilaton field in the emergent metric scenario under  $S^{I}$  compactification.

#### III. QUINTESSENCE

SCALAR DYNAMICS IN HIGHER DIMENSIONAL EINSTEIN GRAVITY: We revisit the domain of observational cosmology to reiterate a variable vacuum energy density in our universe. A time variation of



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cosmological vacuum energy density in the early epoch leading to a de Sitter geometry has been argued in the inflationary models [25, 26, 27]. Remarkably a hidden fifth essence, i.e. a quintessence, is known to describe a time varying spatially homogeneous cosmic density with a negative pressure and a positive energy density. Quintessence is indeed a potential candidate to describe the dark energy in our universe. In the recent past a slowly rolling time dependent scalar field is believed to describe the quintessence presumably due to its simplest form as a tensor field which couples minimally to Einstein gravity [28, 29]. The acceleration of universe is known to be parameterized by the cosmological equation of state:  $\omega = P/\rho$ , where  $P = -T_i^i < 0$  and  $\rho = T_0^0 > 0$  respectively define the pressure and energy density sourced by a scalar field. In the recent years the observational cosmology primarily focuses on the measurement of  $\omega$  sourced by a quintessence. Its value is known to be bounded, i.e.  $-1 < \omega < -1/3$ .

**AXIONIC SCALAR IN A GRAVITATIONAL PAIR:** In the context the quintessence energy density underlying a five dimensional geometric torsion on S<sup>1</sup> has been explored in a string-brane model [12, 13, 14]. It was shown that the non-trivial torsion curvature scalar K has been shown to be sourced by a mass-less axion on an anti  $D_3$ -brane. In particular, the action (5) underlying a vacuum created gravitational pair of  $(3\overline{3})$ -brane reveals that the emergent 3-brane can be governed by a geometric Lorentz scalar  $F^2$  while an anti 3-brane can be described by the curvature scalar K or vice-versa. Then the two within the three local degrees of the five dimensional NS field would like to describe an emergent metric fluctuation on a 3-brane. The remaining local degree underlying an axionic scalar on an anti-3-brane becomes hidden to the emergent (3+1)-dimensional brane universe. Thus a dynamical axion on an anti-brane indeed influences our brane-world. In other words, an axion may naturally be identified with a quintessence scalar in a string-brane model which describes a vacuum created gravitational pair of (3 $\overline{3}$ )-brane.

An extra fifth spatial dimension is transverse to the vacuum created gravitational pair of  $(3\bar{3})$ -brane universe. It is known to be sourced by a higher dimensional gauge field and in the case it is a KR field on a  $D_4$ -brane in a string-brane setup. An axion is Poincare dual to a torsion on a gravitational anti 3-brane and hence is inaccessible to an observer on a vacuum created 3-brane. The idea of a quintessence energy density sourced by an axion field on an anti-brane is remarkable. The dynamical aspects of an axion on a 3-brane universe may also be viewed via an extra fifth dimension in between the gravitational pair, which in turn is known to describe a Liouville scalar in string theory.

A fact that the dark energy permeates all the space and tends to enhance the rate of expansion of universe may be understood via an extra dimension between a vacuum created pair of  $(3\overline{3})$ -brane. Hubble's law may be revisited to explain the receding of a brane universe from an anti-brane. The law states that the recessional speeds of a brane and anti-brane universes are proportional to the transverse distance between them. Since a vacuum created brane universe moves away from its an anti-brane in an opposite direction, it implies a repulsive gravity between them. The notion of repulsive gravity has been argued to be sourced by a quintessence scalar field in cosmology. It provokes thought to believe that an axion in a hidden anti-brane is realized through a geometric torsion which in turn is responsible for the repulsive gravity. In fact a repulsive gravity underlying a quintessence has been conjectured between a matter and antimatter which may seen to be in conformity with the notion of a vacuum created pair of  $(D\overline{D})_3$ -brane by a KR field quanta on a  $D_4$ -brane. Interestingly an effective Schwarzschild de Sitter black hole obtained in a gauge choice for a non-propagating torsion in ref.[30] has been shown to describe a varying positive curvature scalar  $R = 12/r^4$ .

It further strengthens the presence of quintessence axion in a string-brane model. It may imply that the brane/anti-brane universe(s) at its vacuum creation, i.e. at the past horizon radius *b* with a Big Bang, was described by a constant curvature  $R = 12/b^4 > 0$ . Computations [31] have been performed to show that the quintessence kinetic energy can be ignored at the Big Bang and hence the equation of state reduces to  $\omega = -1$ . The result is in agreement with the value of  $\omega$  known for a constant vacuum energy density [28, 29].

**D-INSTANTON AS A QUINTESSENCE:** An axion in the Ramond-Ramond (RR) sector of type II superstring ensures the significance of a *D*-instanton in the string-brane model. Importantly a D-instanton is known to incorporate a non- perturbative correction in a perturbative string theory. In fact the universe was argued to begin at a past horizon with a Big Bang on a pair of  $(D\overline{D})$ -instanton at an early epoch in de Sitter underlying a geometric torsion [12]. The hot de Sitter is believed to expand and the notion of a real time was incorporated subsequently into the geometry. The expansion of a pair of brane (or anti-brane) universe from its origin at the Big Bang singularity was argued to pass through a series of nucleation of a pair of *D*-instanton followed by higher dimensional pairs such as *D*-particle, *D*-string



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and *D*-membrane. The nucleation process stops when a pair of  $(3\overline{3})$ -brane is created as the pair with a transverse fifth dimension completely fills the  $D_4$ -brane world-volume.

In other words an instanton local degree on an anti  $D_3$ -brane influences the world-volume of a  $D_3$ -brane within a pair. Arguably the instantaneous effect of a *D*-instanton on a  $D_3$ -brane is in agreement with the non-perturbative universe in 4*D*. A quintessence axion, presumably on a vacuum created 3-brane, is argued to source an extra fifth dimension to our brane universe on a 3-brane with a vacuum pair. The curvature scalar *K* on a gravitational anti 3-brane may describe a quintessence axion and a geometric  $\mathcal{F}_2$  governs the torsion curvature on a gravitational 3-brane. An accelerated and expanding universe in the present day cosmology may seen to be influenced by a growth in extra dimension between a brane and an anti-brane universes. The high energy torsion modes have been argued to decouple with a large fifth dimension and eventually a low energy brane universe may appear to decouple from the anti-brane in the limit. The decoupling of non-perturbative quantum effects may lead to describe Einstein vacuum in the string-brane model.

Furthermore the brane geometries have been shown to be sourced by an axionic scalar underlying a vacuum created gravitational pair of  $(3\overline{3})$ -brane. They were argued to describe the degenerate vacua and the degeneracy is sourced by a string charge underlying a *NS* field in the string bulk [32, 33, 34]. In principle the degeneracy may seen to be sourced by a lower form obtained from a higher form on  $S^{l}$  or on  $S^{l} \times S^{l}$ . The degenerate brane vacua at string scale may intuitively be identified with the notion of lower dimensional *D*-brane within a higher dimensional brane. The quantum effects have been worked out to show that the low energy perturbative string vacuum receives a non-perturbative *5D*-brane world-volume correction in the string-brane model. Axionic sourced quantum geometries are further analyzed for two larger length scales to qualitatively describe a laboratory black hole in a medium energy regime and a semiclassical brane universe in a low energy regime [34]. Analysis under the emergent metric scalings have been performed to explore the effective (Anti) de Sitter brane vacua in presence of non-perturbative correction(s). A quantum correction has been shown to be approximated by a varying energy density underlying an axionic quintessence.

Thus an axion quanta can vacuum create a pair of  $(D\overline{D})$ -instanton which is the fundamental building block to describe a natural pair of  $(D\overline{D})$ -string by the KR field quanta. The nucleation of a higher dimensional pair of brane/anti-brane ceases with a stable pair of  $(D\overline{D})_3$ -brane underlying a five dimensional gauge theory.

## IV. CONCLUDING REMARKS AND RESULTS

We have briefly reviewed a geometric construction underlying a string-brane model to address an unresolved puzzle in quantum cosmology. In particular the model has been known to incorporate a non-perturbative quantum correction to the low energy string vacuum. Schwinger pair production mechanism was invoked to argue for a vacuum created gravitational pair of  $(3\bar{3})$ -brane at the cosmological horizon by a KR field quanta in the world-volume gauge theory on a  $D_4$ -brane. A stable pair of brane and anti-brane universe has been known to be separated by extra transverse dimension(s) in a ten dimensional superstring theory. They are believed describe the transverse scalars hidden to our brane-universe. One such hidden scalar in a string-brane toy model has been identified with a dynamical axion on an anti 3-brane within a vacuum created pair. The axion was argued to describe the quintessence in the model which is believed to be a potential candidate for dark energy in our universe. However the quintessence axion in the string-brane model is known to source a D-instanton which in turn incorporates non-perturbative correction to our present day universe. At an early epoch, i.e. right after a Big Bang, our universe is believed to be influenced significantly by a non-perturbative quantum correction sourced by an axion in the string-brane model. Primarily the quantum corrections have been known to be described by a geometric torsion which forms a condensate in a low energy regime such as Einstein vacuum.

Furthermore the brane-world models have been successful to address the issues related to the cosmological inflation [25, 26, 27]. These models have been explored to describe the inflationary cosmology underlying a rapid accelerated expansion of our universe [30, 31]. Interestingly a quintessence axionic scalar dynamics is hidden or outside the 4D brane or anti-brane universe in the proposed string-brane model. The axion was argued to source a D-instanton which in turn incorporates a non-perturbative quantum correction to Einstein vacuum. An emergent pair of gravitational brane and anti-brane universe are non-BPS and they may be viewed via a spontaneous supersymmetry breaking phenomenon as they possess their origin in a supersymmetric or BPS  $D_4$ -brane. Thus the massless KR field regains mass, and renamed as a NS field, in an emergent supersymmetry broken phase underlying the gravitational dynamics. The massive NS field further reassures Newtonian gravity which is indeed a non-relativistic limit in Einstein gravity.



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Intuitively, the dark energy sourced by boson(s) and the dark matter sourced by fermion(s) are intimately related by a plausible supersymmetry in a higher dimensional gauge theory. It was shown that a geometric torsion dynamics in a second order formalism leads to an effective space-time curvature scalar K on  $S^{l}$  [12, 13, 14] which may ensure an underlying T-duality symmetry between the gauge theory and the emergent gravity dynamics. Nevertheless the novel idea leading to our proposition for an emergent, non-BPS, stable pair of gravitational 3-brane and anti 3-brane universe inspires thought and possibly sheds light to a non-perturbative formulation such as M -theory [17] and needs further attention in current literature. Our analysis signifying an emergent geometric torsion curvature, underlying a vacuum created gravitational pair of  $(3\overline{3})$ -brane by a KR field quanta, appears to be an insightful tool to explore the cosmological domain related to the accelerated expansion of our universe.

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