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QoS Aware Vertical Handover Decision Algorithm in Heterogeneous Wireless Network

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ABSTRACT: The next generation wireless network is characterized by multi-interface terminals and integration of different network interfaces for providing different types of services. In such a heterogeneous environment, the most important issue is Always Best Connected (ABC) concept. It allows the best connectivity to services anywhere any time and ensures optimum level of Quality of Service (QoS). For that, a seamless inter-system handover solution is needed. One of the challenging problems for the vertical handover is the decision for a mobile node to handover between different types of networks. In this paper we propose a multi-criteria vertical handover decision algorithm for heterogeneous wireless network environment where each interface would provide different services as well as constraints. An intelligent approach based on Particle Swarm Optimization (PSO) has been used for the decision of handover to the most suitable network for a particular application.

KEYWORDS: Wireless communication, Quality of Service (QoS), traffic class, Particle Swarm Optimization (PSO), vertical Handover

I. INTRODUCTION

Technological advancements in the area of wireless communications have provided numerous wireless network technologies such as Bluetooth, Wi-Fi, Wi-Max, GPRS and CDMA. These networks were developed individually to meet specific service requirements. They are distinguished by their own advantages and drawbacks. For example, Wi-Fi networks offers high bandwidths. But due to short coverage provided by Wi-Fi, it is suitable for short range applications such as internet connectivity from personal computer, or a game console; All these applications are subject to a successful wireless connection.

Third generation cellular networks such as UMTS, GSM and CDMA 2000 provide large coverage but the data rates offered by these networks are limited. Satellite networks offer large coverage but deployment is too expensive to be borne by the normal mobile users. Wi-Max networks which can operate in both licensed and unlicensed frequencies, offer higher bandwidth and greater range as compared to Wi-Fi based wireless systems. But it has the drawbacks of installation and operation costs and lack of quality of service.

All these wireless networks have their own merits and limitations. No single wireless network is there which can serve all types of services with equal quality. Next generation (NG) wireless networks or Heterogeneous wireless networks are the integration of various wireless networks so that the best of each of them can be provided to the user. With this interoperability, the user with its handheld mobile terminal (MT) would have complete flexibility to go for any application of its choice and that too with high QoS rating, so that users' satisfaction is achieved by means of an Always Best Connected mode [2-4].

Seamless mobility support across heterogeneous wireless networks is one of the most important research issues. In this context, design of an efficient vertical handover decision algorithm that enables the multi-mode terminal to choose the best among the available networks is of great importance. This paper presents a vertical handover decision algorithm for multi-mode terminals using Particle Swarm Optimization (PSO). It considers terminal characteristics such as Quality of Service (QOS) requirements of the application and the speed of the mobile station.



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II. RELATED WORK

Vertical handoff has so far been a wide area of research. Different algorithms considering different aspects of handoff have been proposed in ([1], [5], [6], [9]-[13], [16]). M. Kassar, B. Kervella, and G. Pujolle [5] give an overview of the vertical handoff decision strategies. Qingyang Song, Abbas Jamalipour [6] gives an idea of QoS negotiation when there is a need of vertical handoff. Shantidev Mohanty and Ian F. Akyildiz [7] discuss about cross-layer handoff which is not actually vertical handoff but they provide a good estimation technique of handoff metrics like handoff-failure probability, false-handoff-initiation probability etc. Liu Xia, Ling-ge Jiang and Chen He [11] proposed a novel fuzzy-quantification based vertical handoff algorithm with differential prediction and pre-decision method. They claim their algorithm may solve the ping-pong effect of handoff decision. Dong Ma, Maode Ma [12] derived an evaluation algorithm to estimate the condition of the available network in terms of bandwidth and packet delay. Handover decision was taken based on the result. Wang Nan, Shi Wenxiao, Fan Shaoshuai, Liu Shuxiang [13] used PSO (Particle Swarm Optimization) as a tool to decide about the initial weight assigned to the hidden layer neurons. Vasu, K, Maheshwari, S. ; Mahapatra, S. ; Kumar, C.S. [15] gives a fuzzy-rule based vertical handoff decision algorithm where the fuzzy-rule base system takes the decision about the target network. Jansie McNair, Fang Zhu give a comprehensive survey of vertical handoff strategies in [14]. K. Radhika, and Dr. A. Venugopal Reddy [16] proposed a vertical handoff decision strategy based on game theory.

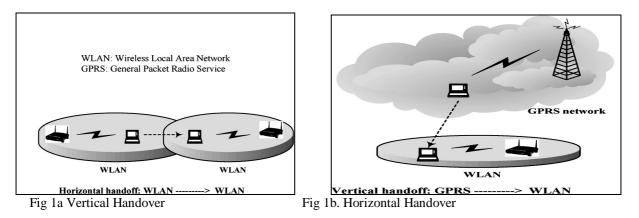
In all these literatures, especially in ([11], [13]) some weights are assigned to the QoS parameters. The weights are assumed randomly irrespective of any extra emphasis given to the dominating parameter for a particular application. This may lead to QoS degradation.

In this paper a QoS aware PSO based vertical handover decision algorithm has been proposed where effort has been made to assign weights to the QoS parameters depending on their respective importance for a particular application.

III. METHODOLOGY

A. OVERVIEW OF HANDOVER PROCESS AND VERTICAL HANDOVER

Handover is the process of maintaining a user's active sessions when a mobile terminal changes its connection point to the access network (called "point of attachment"), for example, a base station or an access point. Depending on the access network that the point of attachment is part of, the handover can be either horizontal or vertical [1]. A horizontal handover takes place between points of attachment supporting the same network technology, for example, between two neighboring WLANs as shown in Figure 1b..



On the other hand, a vertical handover occurs between points of attachment supporting different network technologies, for example, between a WLAN and GPRS network as shown in figure 1a. VHD (Vertical handover decision) algorithms help mobile terminals to choose the best network to connect to, among all the available candidates.



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B. HANDOVER MANAGEMENT PROCESS

There are three steps of handover management processes [5] . They are

Handover Initiation: This phase actually collects the available system information that would be needed for making the decision for handover. The information includes the Received Signal Strength (RSS), available Bandwidth, handover latency and other data from neighboring wireless networks.

Handover Decision: This phase is used to determine whether and how to perform the handover by selecting the most suitable access network based on the information collected in the Handover Initiation phase. This module gives instructions to the execution phase about the target network for optimum handover. It is also called network or system selection.

Handover Execution: This phase is used to change networks conforming to the details resolved during the decision phase. This phase incurs some delay due to the actual handover processed.

In this paper an algorithm has been proposed for the second phase, that is, Handover Decision phase.

C. VERTICAL HANDOVER DECISION FUNCTION

The general function of computing the merit figure [6] of network n is

$$F_n = E_n \sum_i w_i N(p_{n,i})$$

Where $p_{n,i}$ is the *i*th QoS factor in network n, w_i is its corresponding weight, E_n is the elimination factor of network n and N is a normalization function. The value of E_n is decided by the user's mobility, service classes and network characteristics. For example, when the user is in the coverage of WLAN, E = 0 if the user's velocity is more than 7 km/h (pedestrian's maximum speed); otherwise, E=1. The purpose of normalization is to combine various QoS factors in the merit function. A logarithm-based normalization method is widely accepted by the researchers. Suppose only bandwidth and delay are considered for comparisons and the weights of these are $w_{bandwidth}$ and w_{delay} . According to

this concept the merit function may be of the following form

$$F_n = E_n(w_{bandwidth} \cdot \ln p_{n,bandwidth} + w_{delay} \cdot \ln \frac{1}{p_{n,delay}})$$

 $\sum_{i} w_{n}$, i = 1 where i' are the QoS parameters for the *n*th network

D. TRAFFIC CLASSES

Conversational Traffic: The typical applications of this class are VoIP and video conferencing. Real-time conversation is always performed between peers (or groups) of live (human) end-users. This is the only traffic where the required QoS characteristics are strictly given by human perception. e.g. VOIP application.

Streaming Traffic: When the user is looking at (listening to) real-time video (audio), the scheme of real-time streams applies. The real-time data flow is always aiming at a live (human) destination. It is a one-way transport. e.g. CBR application.

Interactive Traffic: When the end-user, that is either a machine or a human, is online requesting data from remote equipment (e.g. a server), this type of traffic applies. Examples of human interaction with the remote equipment are: Web browsing, database retrieval, server access. Examples of machines interaction with remote equipment are: polling for measurement records and automatic database enquiries (tele-machines). e.g. MCBR application.

Background Traffic: When the end-user, that typically is a computer, sends and receives data-files in the background, this type of data transmission is called background traffic. Examples are background delivery of e-mails, SMS, download of databases and reception of measurement records. e.g. FTP application

E. PARTICLE SWARM OPTIMIZATION (PSO)

PSO is a population-based stochastic optimization technique, developed by Dr. Eberhart & Dr. Kennedy. The problem is to determine the *global optimum* (maximum or minimum) of a function of n independent variables $x_1, x_2, x_3, \dots, x_n$

, mathematically represented as f(X), where $X = x_1, x_2, x_3, \dots, x_n$ is called the *parameter vector*. If all components

of X assume real values only, then the task reduces to locating a particular point X in the *n*-dimensional hyperspace



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for which the function value f(X) is either a minimum or maximum in the search range. PSO is a multi-agent parallel search technique. The initial population consists of a convenient number of "particles"; particles are conceptual entities that "fly" through the multi-dimensional search space as the algorithm progresses. Each particle *P* has two state variables:

1. Its current position $\vec{X}(t)$

2. Its current velocity $\overline{V}(t)$

The position vector of each particle with respect to the origin of the search space represents a *candidate solution* of the search problem. Each particle also has a small memory comprising:

1. Its personal best position experienced so far, denoted by p(t)

2. The global best position found so far, denoted by g(t).

For each particle, each component of the initial position vector is selected at random from a predetermined search range while each velocity component is initialized by choosing at random from the interval $[-V_{max}, V_{max}]$ where Vmax is the

maximum possible velocity of any particle in any dimension; the initial settings for p(t) and g(t) are taken as

 $\overline{p}(0)$, $\overline{g}(0)$, $\overline{X}(0)$ for all particles. After the particles are initialized, the iterative optimization process begins, where the positions and velocities of all the particles are altered by the following recursive equations (1) & (2), who for the time being assumed to progress in discret (unit) steps. The equations are presented for the *d*-th dimension of the position and velocity of the *i*-th particle.

 X_{id} (t+1) = X_{id} (t) + V_{id} (t+1) (2)

where the algorithmic parameters are defined as :

ω: inertial weight factor that determines the effect of past velocity on present velocity.

 C_1, C_2 : two constant multiplier terms known as "self confidence" and "swarm confidence" which respectively

determine the influence of p(t) and g(t) on the velocity update formula.

 Φ_1 , ϕ_2 : two uniformly distributed random numbers.

In this paper weights used in the merit function are optimized so that optimum network is chosen for a particular application. Weights for different parameters would vary with respect to traffic.

IV. IMPLEMENTATION

A. SIMULATION PARAMETERS

The simulation has been done in MATLAB 2009b. In this paper it is assumed that there are four overlay wireless networks. They are UMTS (Universal Mobile Telecommunication Network), WLAN(Wireless Local Area Network), GPRS (General Packet Radio System) and WiMax. MT is currently located in UMTS. Table 1 shows the simulation parameters details.

Parameter		Value				
Average speed of the node		50m/sec				
Reference distance for RSS		50m				
Cell Radius	of	3000m/100m/300m/100m				
UMTS/WLAN/WiMAX/GPRS						
networks						
Power consumption		0.02w per bit				
Threshold RSS	for	(-100dbm)/(-30dbm)/(-56dbm)/(-				
UMTS/WLAN/WiMAX/GPRS		45dbm)				

Table 1: Simulation Parameters



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Table 2: Network Parameters						
Network	Bandwidth	Packet Delay	Velocity (m/sec)	Bit Error Rate	Jitter (msec)	
	(Mbps)	(ms)		(per 10^8 bit)		
UMTS	0.3	180	30	200	30	
WiMAX	0.8	120	9	150	120	
WLAN	2	160	8	200	200	
GPRS	0.7	70	15	150	170	

Table	2:1	Netwo	ork	Par	am	lete	rs	

	Table 3: Threshold values for QoS						
Bandwidth	BandwidthDelay (ms)VelocityBit Error RateJitter						
(Mbps)	(Mbps) (m/sec)						
0.6	130	7.5	170	70			

Table 4: Cost per bit						
UMTS	WiMAX	WLAN	GPRS			
0.2	0.1	0.4	0.3			

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Table 5: QoS parameters for various traffic classes						
Parameter	Band width	Band width Packet Delay Velocity Bit Error Rate Jitter (mse				
	(Mbps)	(msec)	(m/sec)	(per 10^8 bit)		
Conversational	0.8	220	5	400	60	
Streaming	1.2	280	5	400	60	
Interactive	0.6	300	5	250	200	
Background	0.2	380	5	250	300	

Table 2 is showing the network parameters used in this simulation. Threshold parameters' values for maintain the minimum level of QoS have been put in table 3. Cost per bit incurred by each type of network used is shown in table 4. Table 5 shows the characteristic parameter values for four traffic classes used in this paper. It is assumed that the MT is moving away from the base station of UMTS with an average speed 50m/sec. Every 5 sec the MT is sampling the received signal strength (RSS) and running the algorithm for taking the handoff decision.

B. QOS AWARE VHO ALGORITHM BASED ON PSO:

The proposed algorithm in this paper can be classified as Mobile Controlled Handoff (MCHO) algorithm. It runs in the following steps.

Step 1:

The node, equipped with multiple interfaces, will compare the RSS_{curr}(Received Signal Strength from the current network) with the RSS_{threshold}. If RSS_{current} is less than RSS_{threshold} (mentioned in table 1) of the current network, then the node (MT) will initiate the handoff procedure .

Step 2:

The node, equipped with multiple interfaces, will collect the information about the status of the QoS parameters of the neighboring networks.

Step 3:

The parameter-values obtained on multiple interfaces are associated with different units. They need to be normalized so that they can be uniformly represented in scale [0 1]. For this purpose Eqn. 3 is used.

 $W_{i_n} = (P_{user} - QoS_{threshold}) / (P_{network} - QoS_{threshold}) \dots Eqn. 3$

Where,

- a) Set of parameter values required by the user(P_{user})
- b) Set of parameter values provided by the candidate network (P_{network})



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Set of parameter values required for maintain a threshold quality of service below which the service will be c) disrupted. (QoSthreshold)

Table 2, table 3 and table 5 are used for this purpose. The resulted table after the normalization process is shown in table 6. Each row in the table 5 is considered as Puser

Network	Bandwidth (Mbps)	Packet Delay (ms)	Velocity (m/sec)	Bit Error Rate (per 10^8 bit)	Jitter (msec)
UMTS	0.304569	0.101523	0.182741	0.182741	0.228426
WiMAX	0.140008	0.114552	0.113292	0.113292	0.518855
WLAN	0.225303	0.121317	0.262854	0.075101	0.315425
GPRS	0.212312	0.137378	0.155695	0.069992	0.424623
Step 4.					

Table 6: Weight Matrix (W_{in})

PSO has been applied on the weight matrix. The aim is to maximize the objective function (Eqn. 4) subject to the condition that $\sum w_{i,n} = 1$. Following merit function has been has been considered as objective function or fitness function of PSO.

max

$$F = E_n \sum w_{i,n} \cdot \ln(X_{i,n})^{\text{....Eqn. 4}}$$

Such that $\sum w_{i,n} = 1$

Where X_{in} is the ith parameter of nth network under consideration. If the parameter leaves a positive effect on the Quality of Service then $\ln(X_{in})$ is positive else it is negative [14]. w_{in} is the weight assigned for the parameter

 $X_{i,n}$.

Step 4:

 E_n is the elimination factor. E_n depends on the difference of QoS_{threshold} and P_{network}. If P_{network} is greater than $QoS_{threshold}$ then E_n is 1 otherwise E_n is 0. E_n actually indicates that whether the network in consideration is qualified as target network for the particular application. Puser , QoSthreshold and Pnetwork are vectors consisting of [bandwidth, delay supported, power consumption, bit error rate, jitter]. $W_{i,n}$ gives values less than one but summation of $W_{i,n}$ is 1. The

weight matrix formed with these $W_{i,n}$ values are taken as the initial values to be used in PSO. The aim is to find the optimal set of weights for the network-parameters so that the objective function is maximized and at the same time the fittest network is selected as target of handoff. The fittest network would be associated with the optimum value of the objective function (Eqn. 4).

Step 5:

Outline of PSO based vertical handoff decision algorithm is as follows:

The jth particle position (the network where the MT is currently belonging to) and i) velocity have been assigned randomly throughout the solution space using the following formula:

$$S_0^{j} = S_{\min} + \gamma_1 (S_{\max} - S_{\min})$$
$$V_0^{j} = \frac{S_{\min} + \gamma_2 (S_{\max} - S_{\min})}{\Delta t}$$



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Where r_1 and r_2 are random numbers between 0 and 1, S_{min} is the vector of lower bound and S_{max} is the vector of upper bound.

- ii) Fitness value of the optimization process of the candidate solution is calculated
- iii) The local best value (p_{best}) is searched from the fitness values hitherto calculated. The position vector corresponding to the p_{best} is found i.e the parameter values corresponding to the fitness value
- iv) Now the global best fitness value is obtained and designated as $g_{\text{best.}}$
- v) For each particle the velocity is calculated according to (1) where ω can be calculated as proposed by Shi and

Eberhart [17][18]
$$\omega = \frac{(iter_{max} - iter_{current})^* (\omega_{start} - \omega_{end})}{iter_{max}} + \omega_{end}$$

 $iter_{max}$ is the maximum number of iteration of PSO. $iter_{current}$ is the current value of the iteration.

 \mathcal{O}_{start} and \mathcal{O}_{end} are taken to 0.9 and 0.4 respectively. The 'trust' parameters c1 and c2 are assumed to be of value 2 in (1). Position of the particles are updated according to (2).

vi) The stopping criteria considered here are the number of iteration and the minimum value of fitness obtained from QoS_{threshold}, whichever is reached erlier.

Step 6: PSO suggests about the fittest target network for handoff. This suggestion is passed to the handoff execution phase which actually prepares the system for handoff.

V. RESULTS

One metric called "merit-to-cost ratio" (MCR) is used for comparison of acceptability of different target networks for different traffic classes.

MCR= value of the merit function or objective function in PSO corresponding to the fittest network

cost per bit incurred by the network

The normalized value of this metric is used in the following figures to show the acceptability of a network on the basis of varying requirement. High value of the metric indicates more acceptability. It is seen from Fig. 2 that for conversational traffic the merit-to-cost-ratio is highest for the WLAN network provided that the velocity is less than 8km/h. The metric gives maximum value for GPRS when the application type resembles background traffic (Fig. 4). For streaming traffic UMTS network is selected if bandwidth requirement is not very high as seen Fig. 4. This is the network which supports maximum speed of the Mobile Terminal.

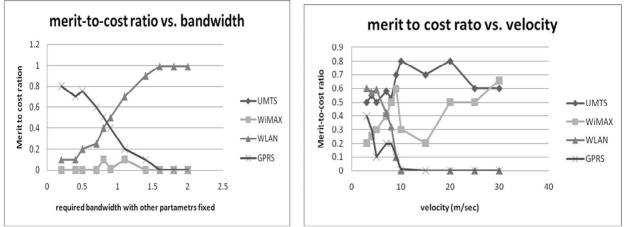


Fig. 2: Bandwidth vs merit-to-cost ratio for conversational traffic where velocity is kept within 8km/h Fig. 3: Velocity vs merit-to-cost ratio for streaming traffic when bandwidth requirement is below 2 mbps.



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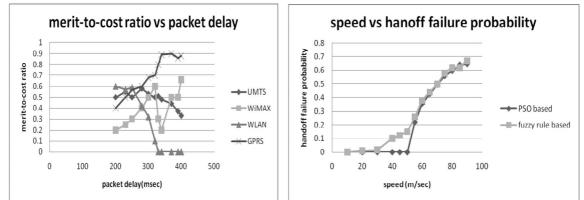


Fig.4 : Packet delay vs merit-to-cost ratio for background traffic Fig. 5: Handoff-failure probability with varying speed of MT

The proposed algorithm is compared with the algorithm based on fuzzy rule based vertical handoff decision algorithm [15]. It is found that with increasing speed of the mobile terminal (MT) leads to a higher probability of handoff failure. Considering this aspect, it is found from Fig. 5 that the two algorithms perform almost similarly when the speed is beyond 55m/sec. The PSO based algorithm performs better below that speed. But if we consider memory requirement of an algorithm as its performance metric then the PSO based algorithm will surely outperform the fuzzy-rule based algorithm. The fuzzy-rule base system will show an exponential increase in the requirement of memory space with addition of every new QoS parameter, whereas in the PSO based algorithm every additional parameter will add an extra column of the parameter matrix.

VI. CONCLUSION

In the PSO based algorithm considered in the present paper only five QoS parameters and four probable type of networks are considered. There remains a huge set of different networks with varied range of parameters which need to be considered for a real life implementation of the algorithm. It is found that the handoff failure probability actually depends on the number of iteration of PSO algorithm. Effort is being made to make a tradeoff between these two aspects of the algorithm so that the handoff failure probability may be independent of the iteration of PSO.

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